

# Prediction and Control of Salt Accumulation in the Upper Root Zone Under Sub-Surface Drip Irrigation

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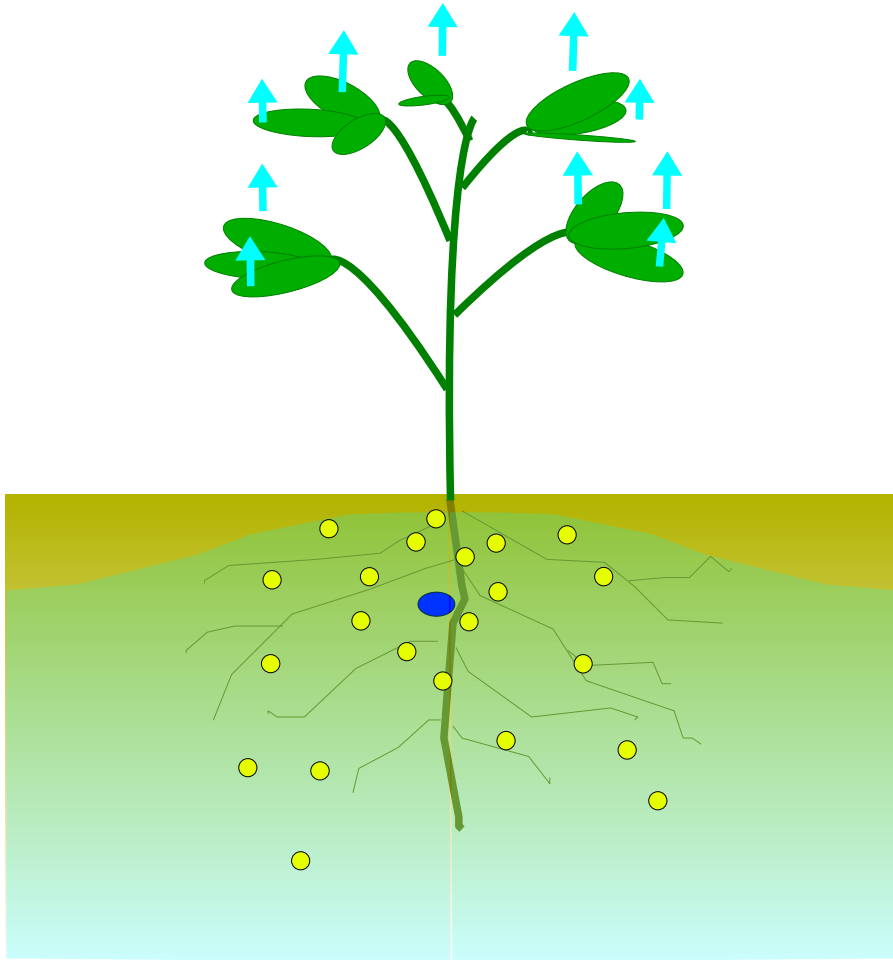
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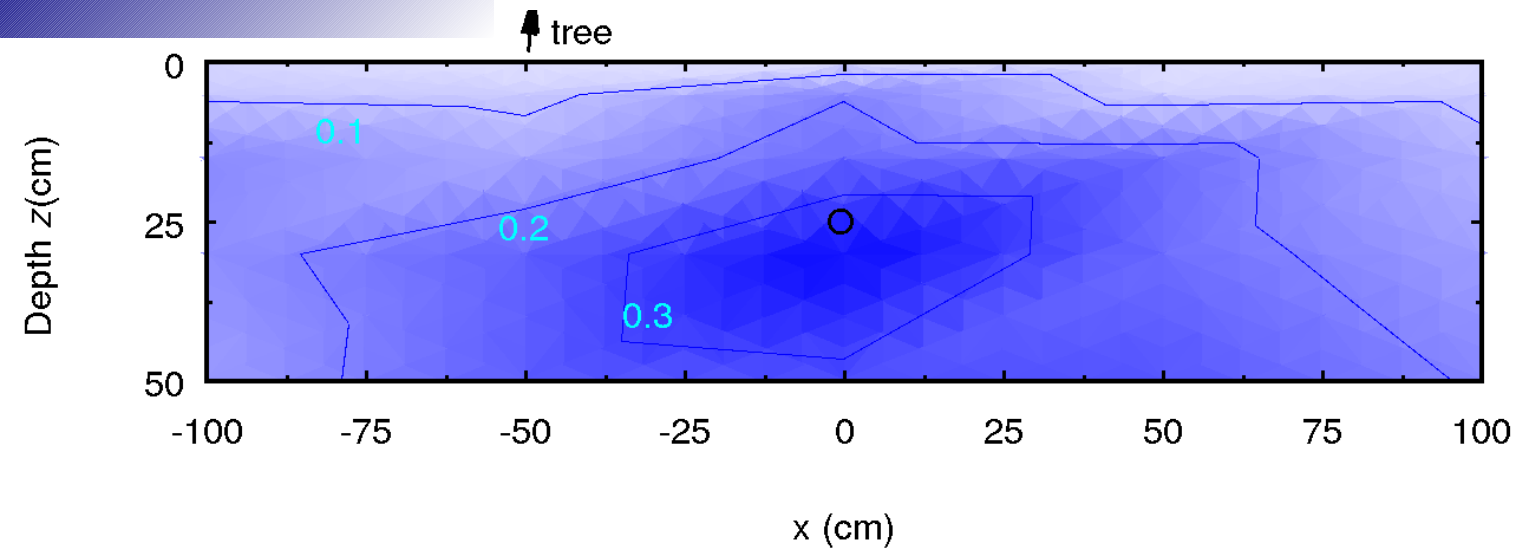
# Introduction

Sub-surface drip irrigation (SSDI) is expected to play a key-role in arid regions as the ultimate water saving method.

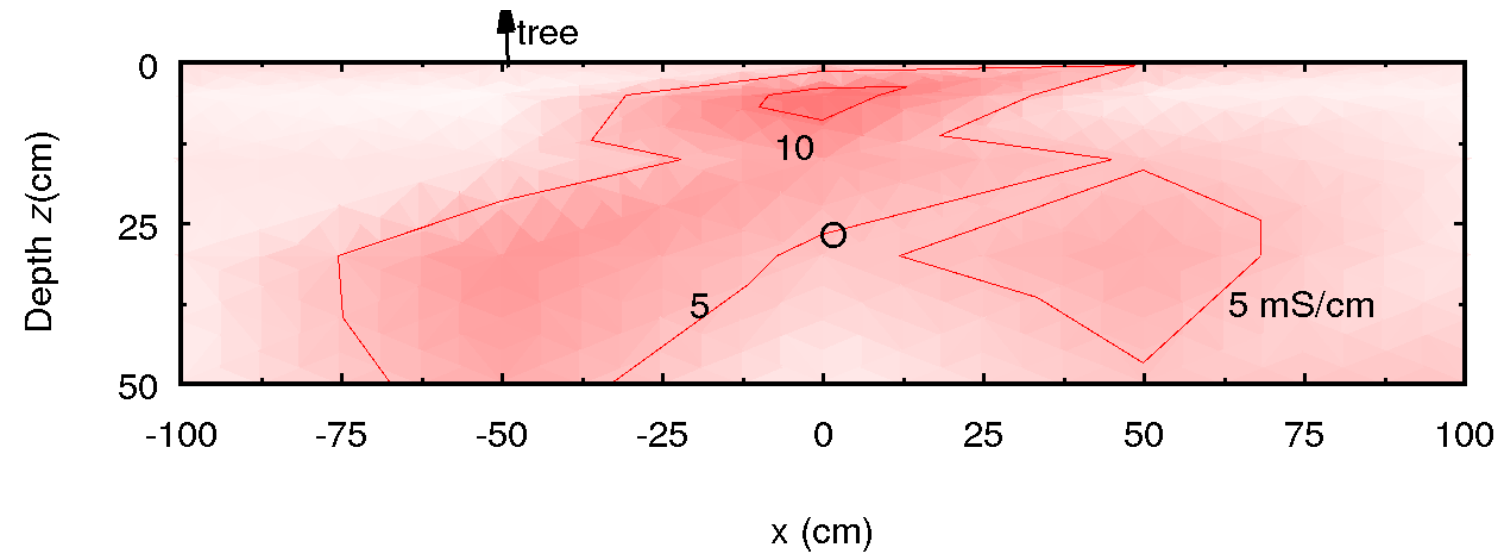


One of the drawback of SSDI: the accumulation of salt to the upper root zone and it cannot be leached out by water from emitter.

# Introduction



Distribution of volumetric water content under subsurface drip irrigation in almond field (under vital tree) at Sa'as kibutsu, Israel



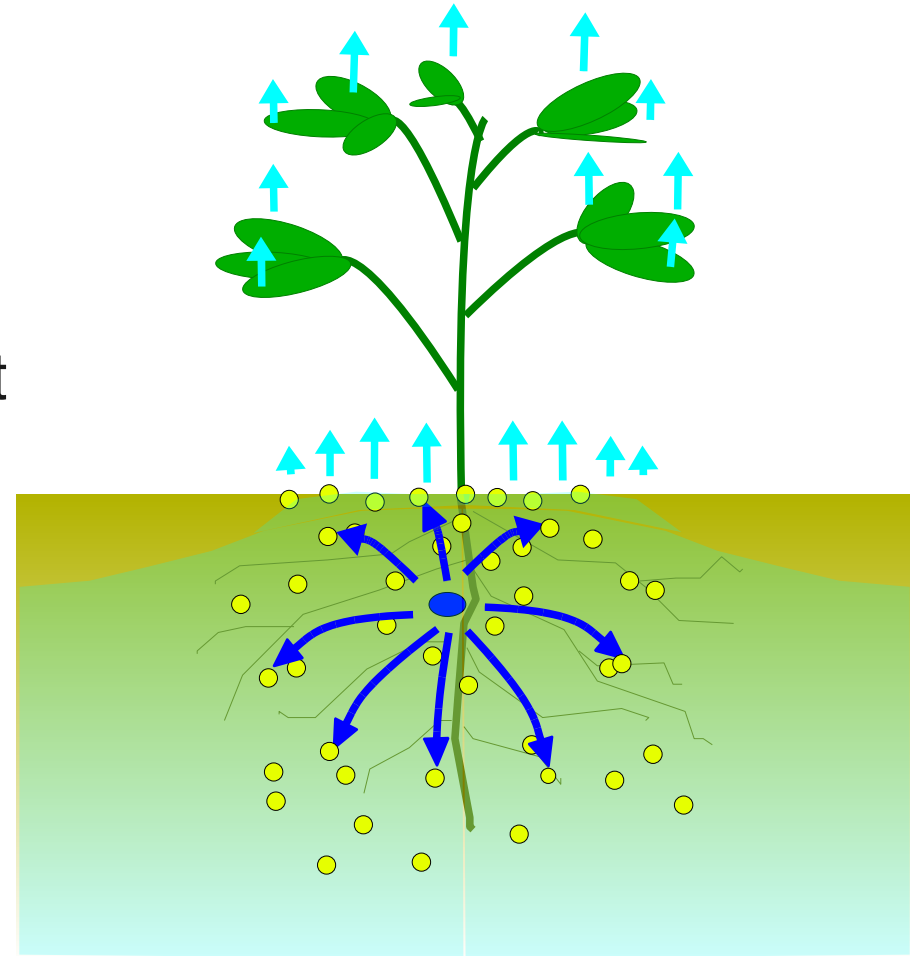
Distribution of electrical conductivity of saturated extract under subsurface drip irrigation in almond field (under vital tree) at Sa'as kibutsu, Israel



# Introduction

## Upward Leaching Method

1. Application of much water enough to make wetting front reach to the soil surface
2. Scraping of surface layer after salt accumulates due to evaporation



# Objectives

- To develop a simulation model for predicting salt accumulation and leaching under sub-surface drip irrigation: i. e. two dimensional movement of water, heat and solute as well as evapotranspiration and root water uptake, **considering the water vapor movement and effect of salt crust on evaporation.**
- To test the validity of the model by comparison with experimental results
- To evaluate the upward leaching method to remove accumulated salt in the upper root zone.

# Materials and Methods

soil: Masa loamy sand  
placed in a greenhouse  
plant: soybean

7/16: seeding

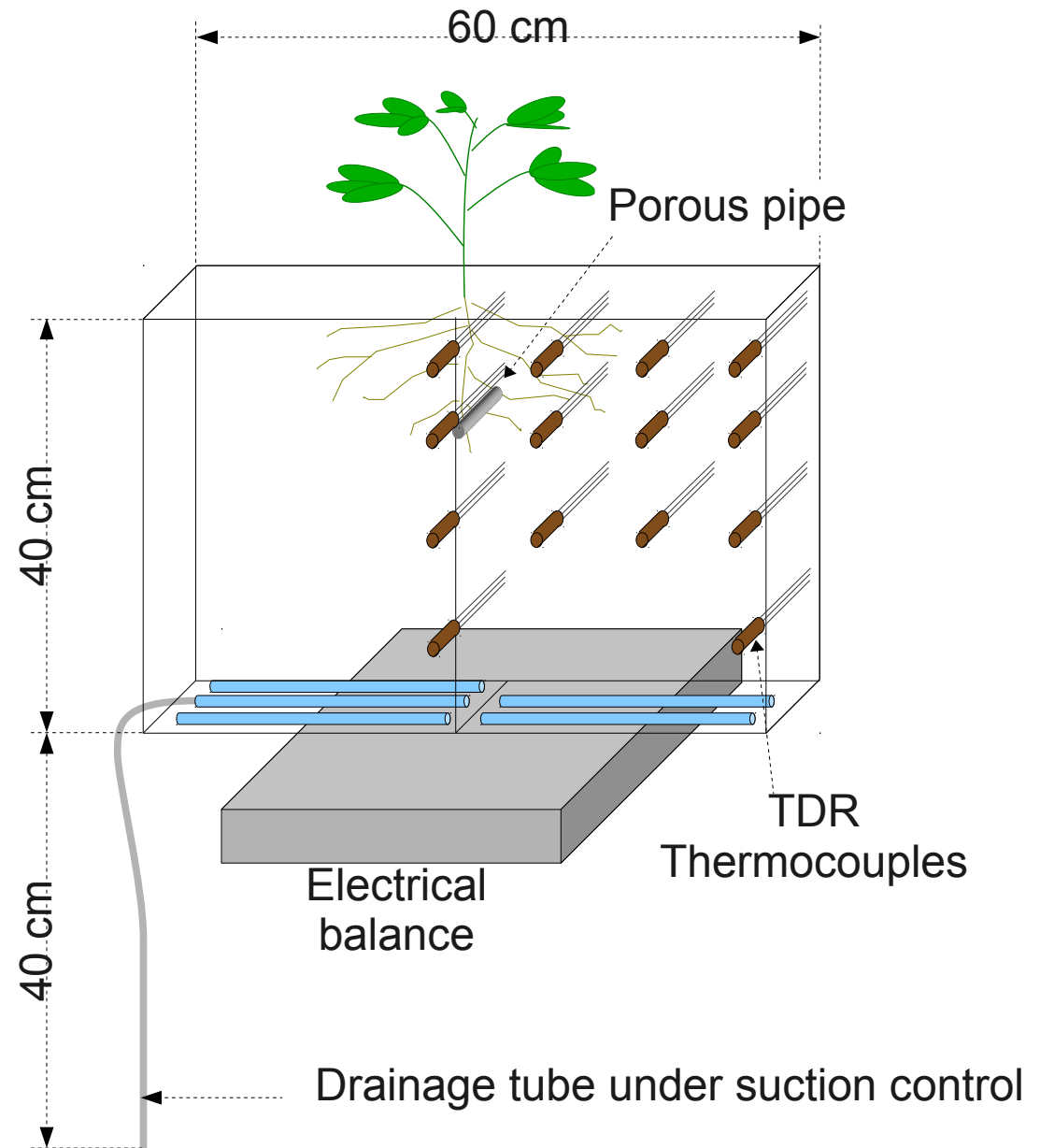
8/15: saturation with tap water

9/ 1: irrigation with 5000ppm  $\text{CaCl}_2$   
solution started

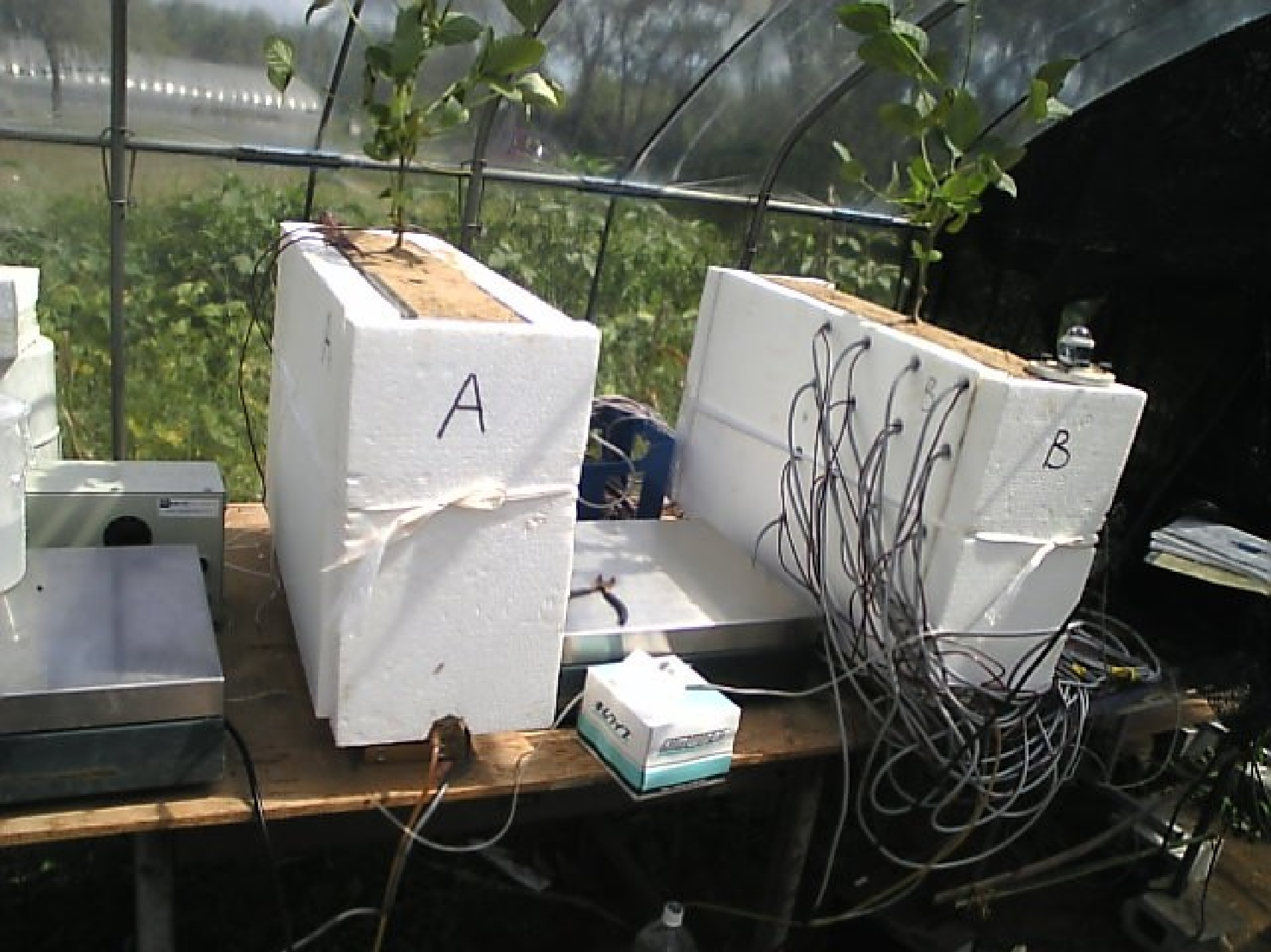
irrigation depth = ET

9/25: upward leaching with 1.7 cm

10/1: scraping and sampling







A

B

MUT

# Numerical Simulation

## Governing equation for water flow

$$\frac{\partial \theta}{\partial t} = - \left( \frac{\partial q_{lx}}{\partial x} + \frac{\partial q_{lz}}{\partial z} \right) - \left( \frac{\partial q_{vx}}{\partial x} + \frac{\partial q_{vz}}{\partial z} \right) + S$$

$$q_{lx} = -K \frac{\partial \psi}{\partial x}$$

$$q_{lz} = -K \left( \frac{\partial \psi}{\partial z} - 1 \right)$$

$$q_{vx} = -a \tau \rho_w^{-1} h_r D_{va} \left\{ \frac{\rho_v^*}{R_v T_s} \frac{\partial \psi_w}{\partial x} + \eta \frac{\partial \rho_v^*}{\partial T_s} \frac{\partial T_s}{\partial x} \right\}$$

$$q_{vz} = -a \tau \rho_w^{-1} h_r D_{va} \left\{ \frac{\rho_v^*}{R_v T_s} \frac{\partial \psi_w}{\partial z} + \eta \frac{\partial \rho_v^*}{\partial T_s} \frac{\partial T_s}{\partial z} \right\}$$

$\theta$ : volumetric water content

$q_l$ : liquid water flux (cm/s)

$q_v$ : water vapor flux (cm/s)

$K$ : hydraulic conductivity (cm/s)

$\psi$ : pressure head (cm)

$\psi$ : matric potential (cm)

$\psi_w$ : water potential (cm)

$a$ : air-filled porosity

$\tau$ : tortuosity

$D_{va}$ : water vapor diffusion coefficient  
in air (cm<sup>2</sup>/s)

$\eta$ : enhancement factor for thermal  
vapor diffusion

$T_s$ : soil temperature (K)

$\rho_v^*$ : saturated water vapor density  
(g/cm<sup>3</sup>)

$h_r$ : relative humidity

$R_v$ : the gas constant for water vapor  
(4697 cm/K)

$S$ : root water uptake (s<sup>-1</sup>)

Numerical Method: Alternative Direction Implicit FDM (ADI)  
with Celia(1990)'s mass-conservative iteration scheme



# Transpiration Rate

## Potential Transpiration Rate ( $T_{rp}$ )

$$T_{rp} = W E_p K_c$$

$W$ : width of the target region (cm)

$E_p$ : ET by Penman equation (cm/s)

$K_c$ : crop coefficient for transpiration

$$K_c = a_{kc} [1 - \exp(b_{kc} \Sigma T dt)] + c_{kc}$$

$a_{kc}$ ,  $b_{kc}$ : plant-specific parameters

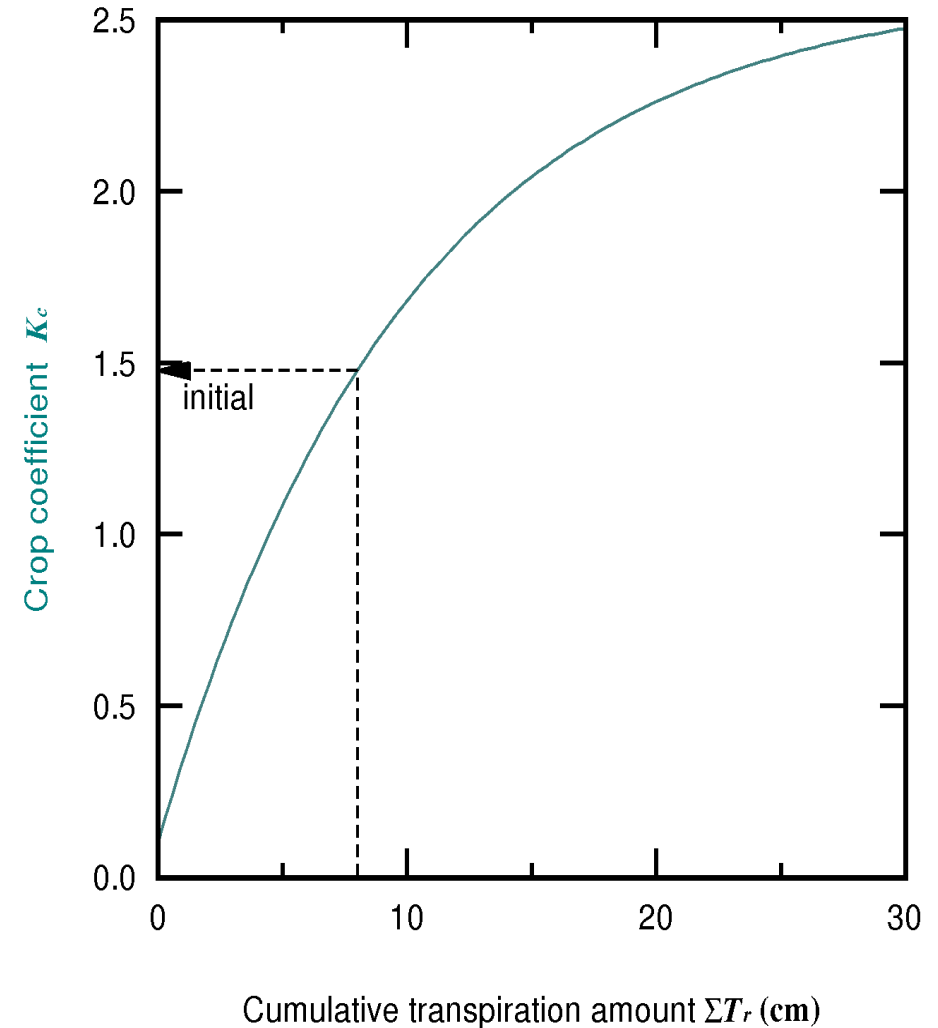
## Actual Transpiration Rate ( $T_r$ )

$$T_r = \int_0^{drt} \int_0^W S dx dz$$

$$S = T_{rp} \beta \alpha_w \alpha_s$$

$\alpha_w$ : reduction coefficient for water stress

$\alpha_s$ : reduction coefficient for salinity stress



Crop coefficient as a function of cumulative transpiration amount

# Root Water Uptake

van Genuchten's response function (1987)

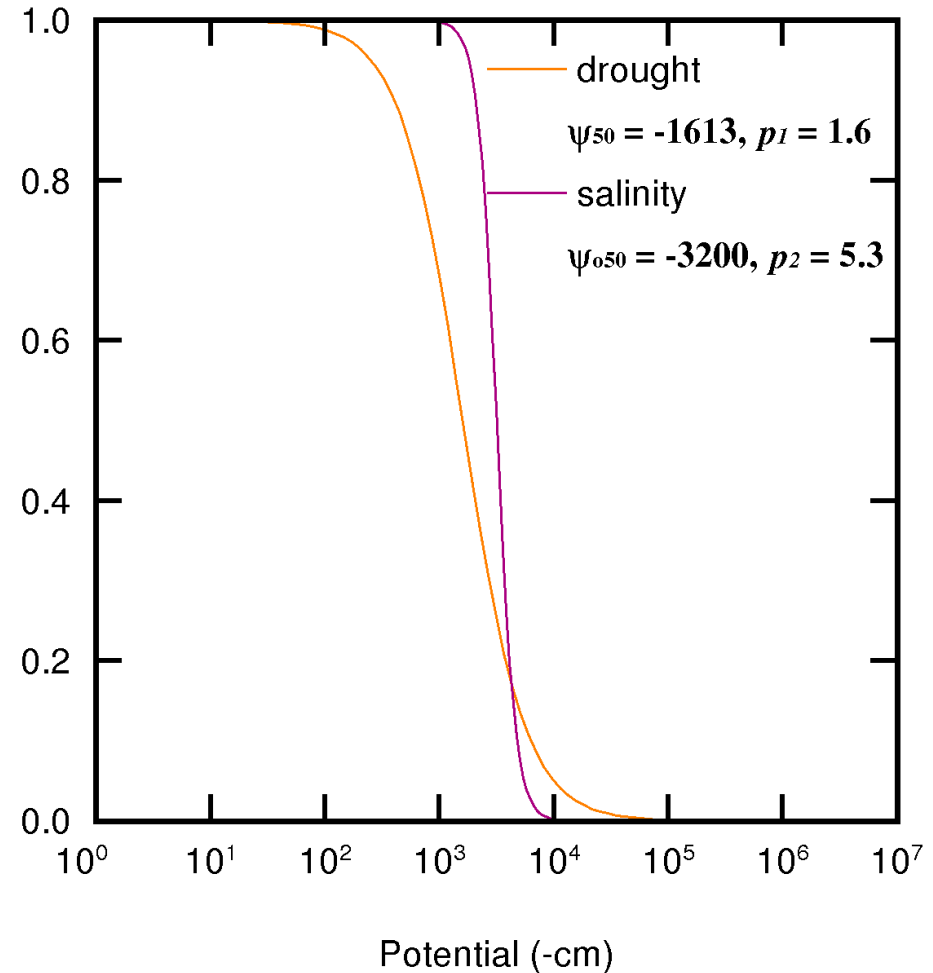
$$\alpha = \alpha_w \alpha_s = \frac{1}{1 + \left( \frac{\psi}{\psi_{50}} \right)^{p_1}} \times \frac{1}{1 + \left( \frac{\psi_o}{\psi_{o50}} \right)^{p_2}}$$

fitting parameters

reduction due to salinity stress

reduction due to water stress

Reduction coefficient  $\alpha$



Drought and salinity stress response function for soybean

## Governing equation for solute movement

$$\frac{\partial(\theta c)}{\partial t} = - \left( \frac{\partial q_{sx}}{\partial x} + \frac{\partial q_{sz}}{\partial z} \right) + S_c$$

$$q_{sx} = -\theta D_{xx} \frac{\partial c}{\partial x} - \theta D_{xz} \frac{\partial c}{\partial z} + q_{lx} c$$

$$q_{sz} = -\theta D_{zz} \frac{\partial c}{\partial z} - \theta D_{zx} \frac{\partial c}{\partial x} + q_{lz} c$$

$$\theta D_{xx} = \theta D_{iw} \tau_s + \frac{\lambda_L q_{lx}^2 + \lambda_T q_{lz}^2}{|q_l|}$$

$$\theta D_{zz} = \theta D_{iw} \tau_s + \frac{\lambda_L q_{lz}^2 + \lambda_T q_{lx}^2}{|q_l|}$$

$$\theta D_{xz} = \theta D_{zx} = \frac{(\lambda_L - \lambda_T) q_{lx} q_{lz}}{|q_l|}$$

$c$  : solute concentration (mg/cm<sup>3</sup>)

$q_s$  : solute flux (mg/cm<sup>2</sup>/s)

$S_c$  : sink/source for solute (mg/cm<sup>3</sup>/s)

$D$  : dispersion coefficient (cm<sup>2</sup>/s)

$D_{iw}$  : diffusion coefficient in free water (cm<sup>2</sup>/s)

$\tau_s$  : tortuosity factor for ionic diffusion

$\lambda_L$  : longitudinal dispersivity (cm)

$\lambda_T$  : traversal dispersivity (cm)

## Conditions for Numerical Simulation

root density distribution: measured one

lower BC: daily-measured cumulative outflow

Thermal vapor diffusion was incorporated by plainly inter/extrapolating measured soil temperature.

Aerodynamic resistance:

given from hourly wind velocity at the nearest weather station with correction factor such that aerodynamic resistance gives daily evaporation rate from wet soil beside the lysimeter.

### Position Information

Soil Layering (unit: cm)

Number of Soil Layer : 1

Depth of 0<sup>th</sup> border = 0

Space Discretization (unit: cm)

Depth of lower boundary = 40

Thickness of 1st element = 0.2

Thickness of bottom element = 2.5

Width of element = 1

Width of the region = 60

Observation Point (unit: cm)

Number of Observation Point : 6

Location of 1<sup>st</sup> obs. point : x = 31  
z = 10

<< Back   Execute   Next >>

### Water Flow Information

Initial Condition

Type : Static profile (equilibrium)

Initial pressure head at the soil surface = -68

Initial hysteretic process :  Drying

Upper Boundary Condition

Type : Variable (cumulative) water flux (using a file)

File name Irrigation\_exp4A.txt

drip irrigation depth of emitter = 12 cm; distance from left end = 30

Left Boundary Condition

Type : impermeable

Lower Boundary Condition

Type : Variable flux

File name CumOutflow\_exp4A.txt

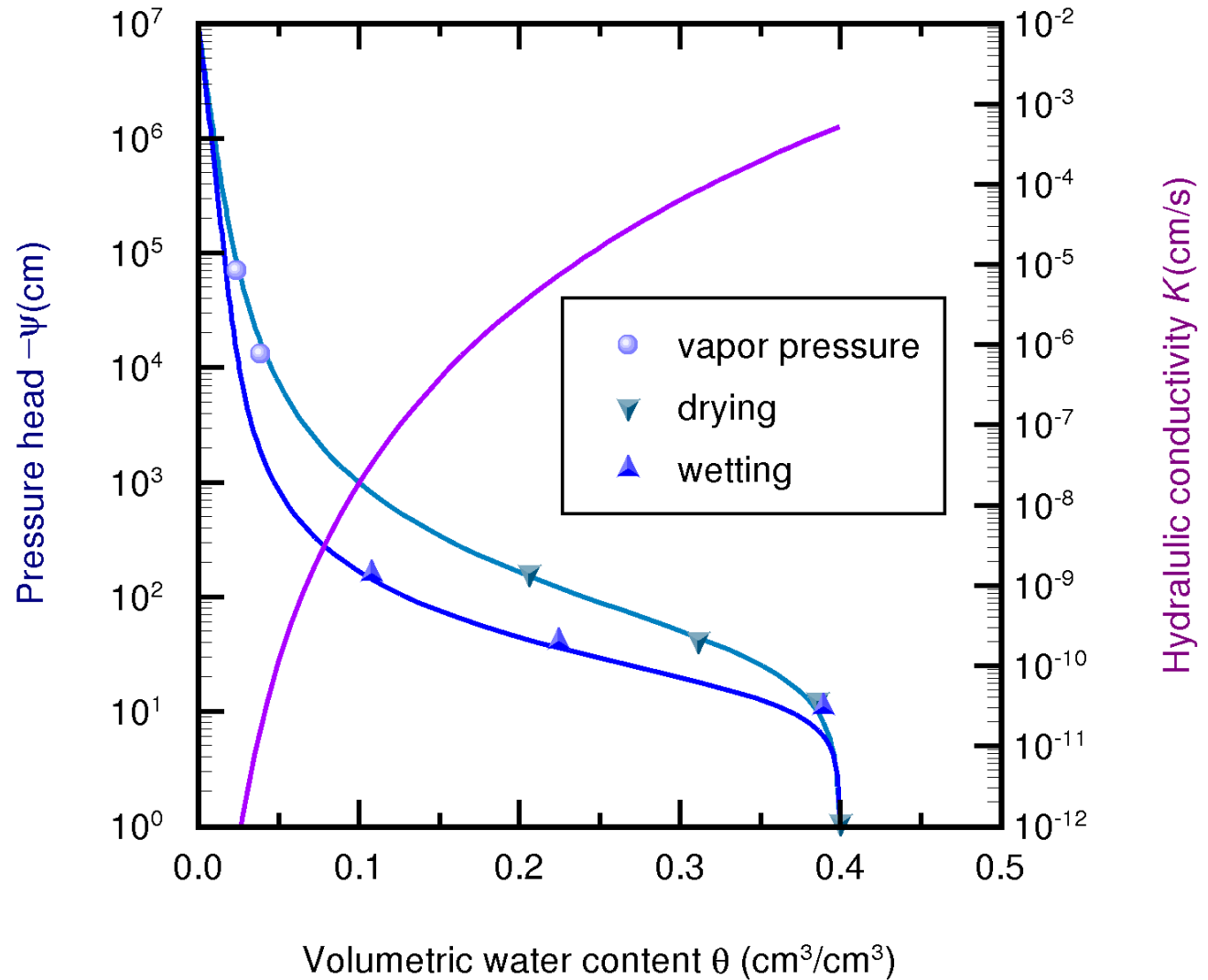
Numerical Detail   << Back   Execute   Next >>

## Hydraulic Properties :

**independently measured** using the hanging water method, the vapor equilibrium method, the transient evaporation method

$$\theta = \frac{\theta_{sat} - \zeta}{\left[ 1 + (-\alpha \psi_m)^n \right]^m} + \zeta \left\{ 1 - \left[ \frac{\ln(-\psi_m + 1)}{\ln(-\psi_0 + 1)} \right]^2 \right\}$$

$$K = K_{sat} \left( \frac{\theta}{\theta_{sat}} \right)^\omega$$

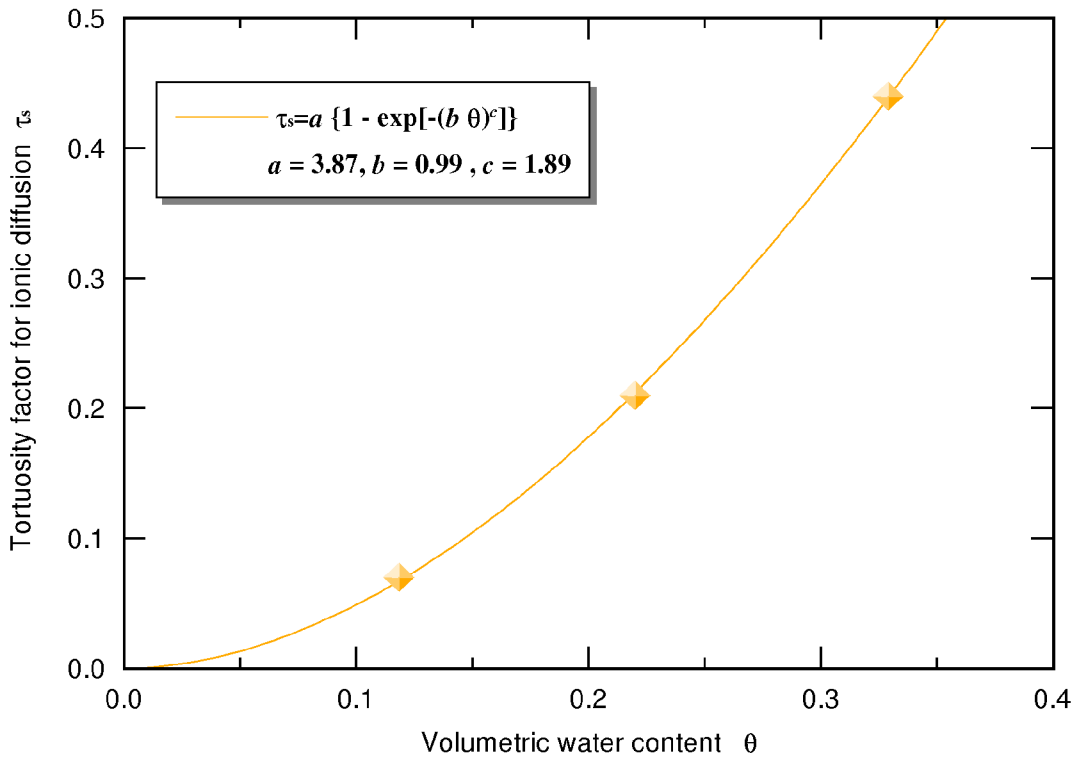


Soil water retention curve of Masa loamy sand

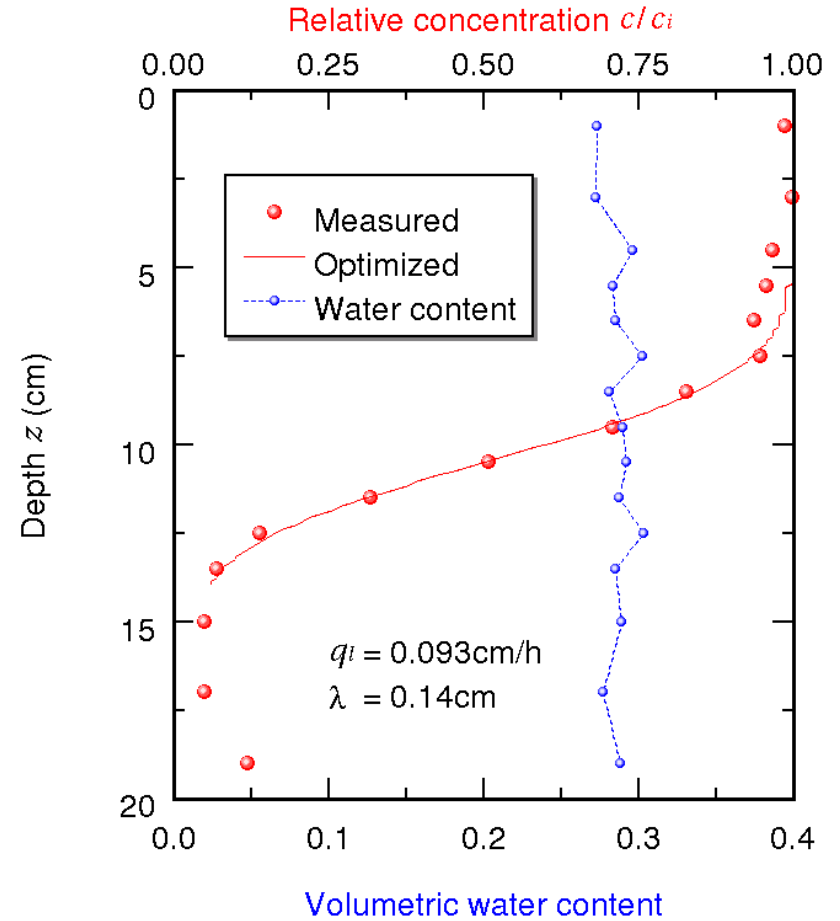


# Solute Transport Properties :

**independently measured** using the half cell method and the long column method (c vs z).



Tortuosity factor for ionic diffusion as a function of water content



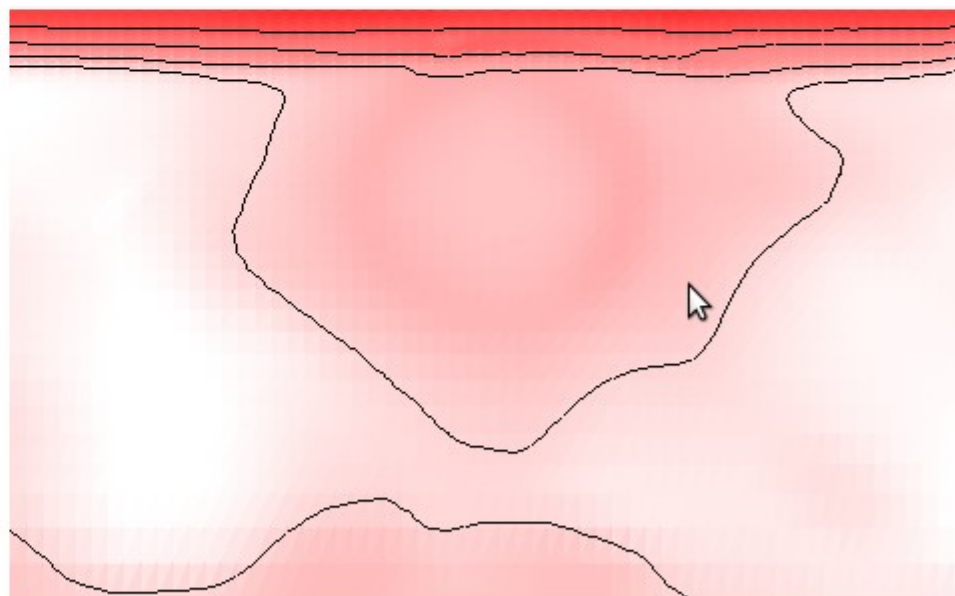
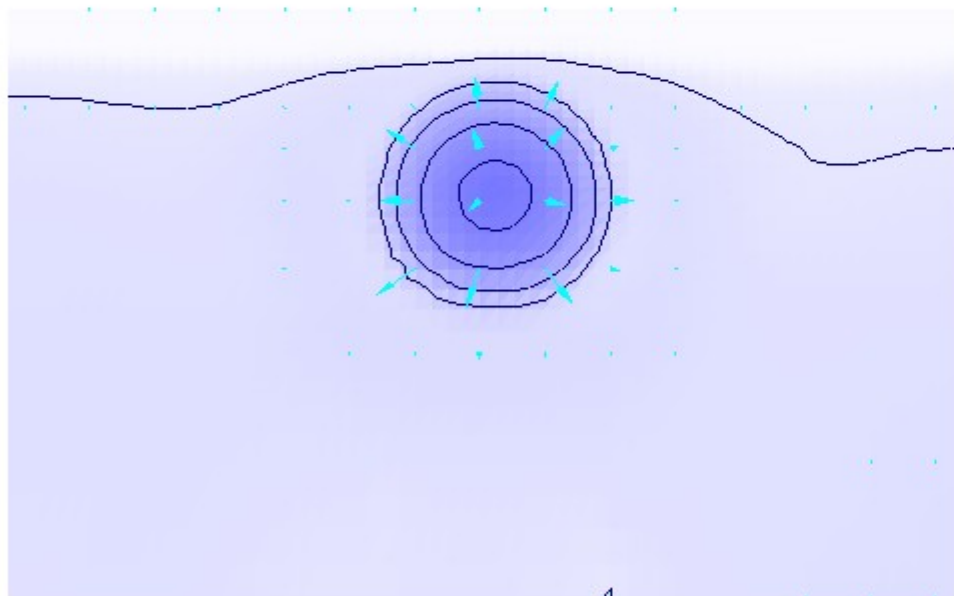
Concentration and water content profiles under the displacement experiment for Masa loamy sand

File Input Execute Help

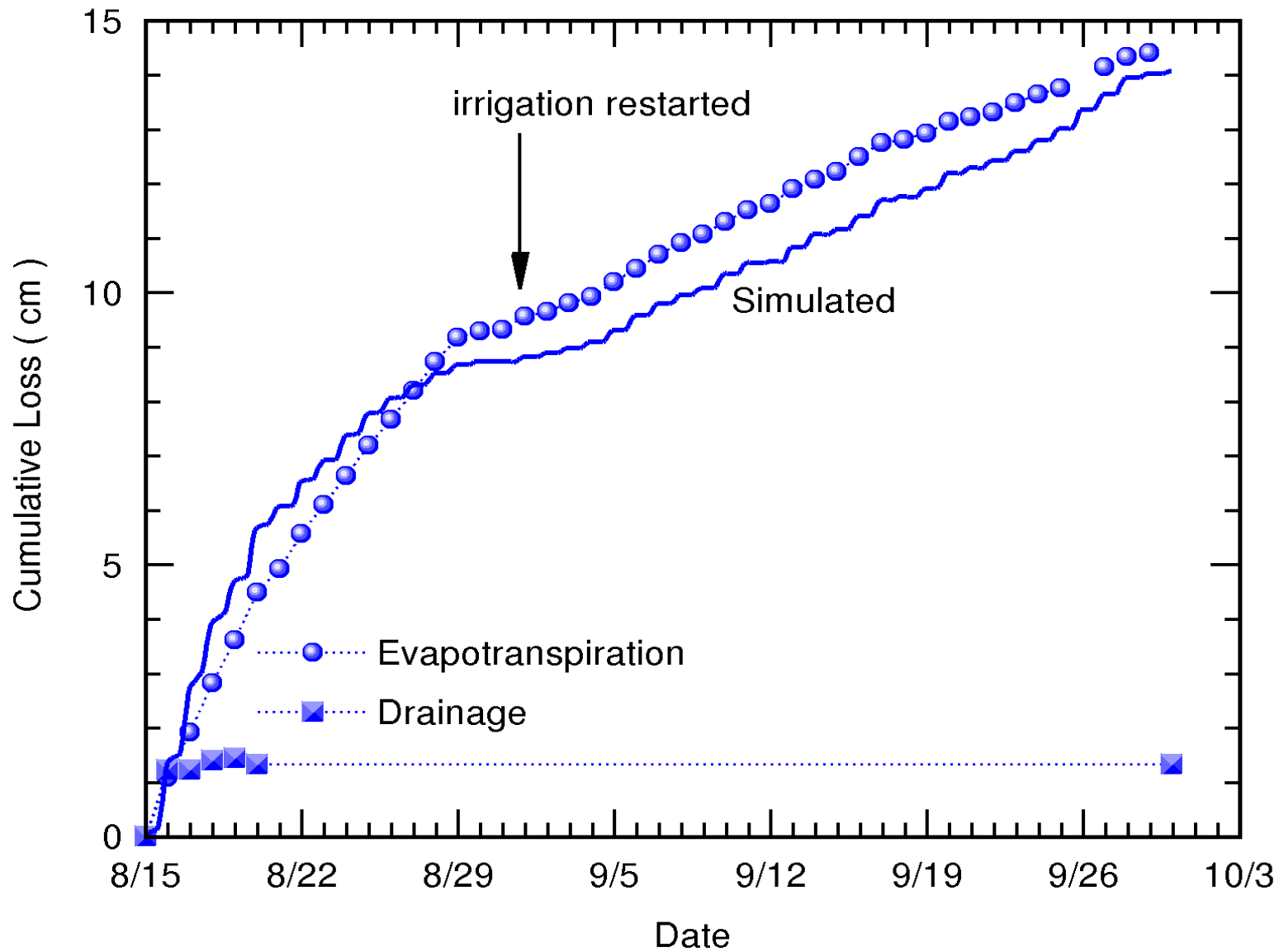


t = 506.001 hour  
water balance error = 0.062%  
cum\_infiltr = 52.49  
cum\_evaporation = 198.37  
cum\_drainage = 79.96  
cum\_leftward\_drainage = 0.00  
cumul. transpiration = 354.93  
cumulative (Tr / Trp) = 0.58  
ini\_storage = 737.59  
storage = 156.36  
W[nx/2,1] = 0.009  
W[nx/2,nz] = 0.056  
W[nx/2,nz/2] = 0.205  
W[nx,1] = 0.009  
W[nx,nz] = 0.067

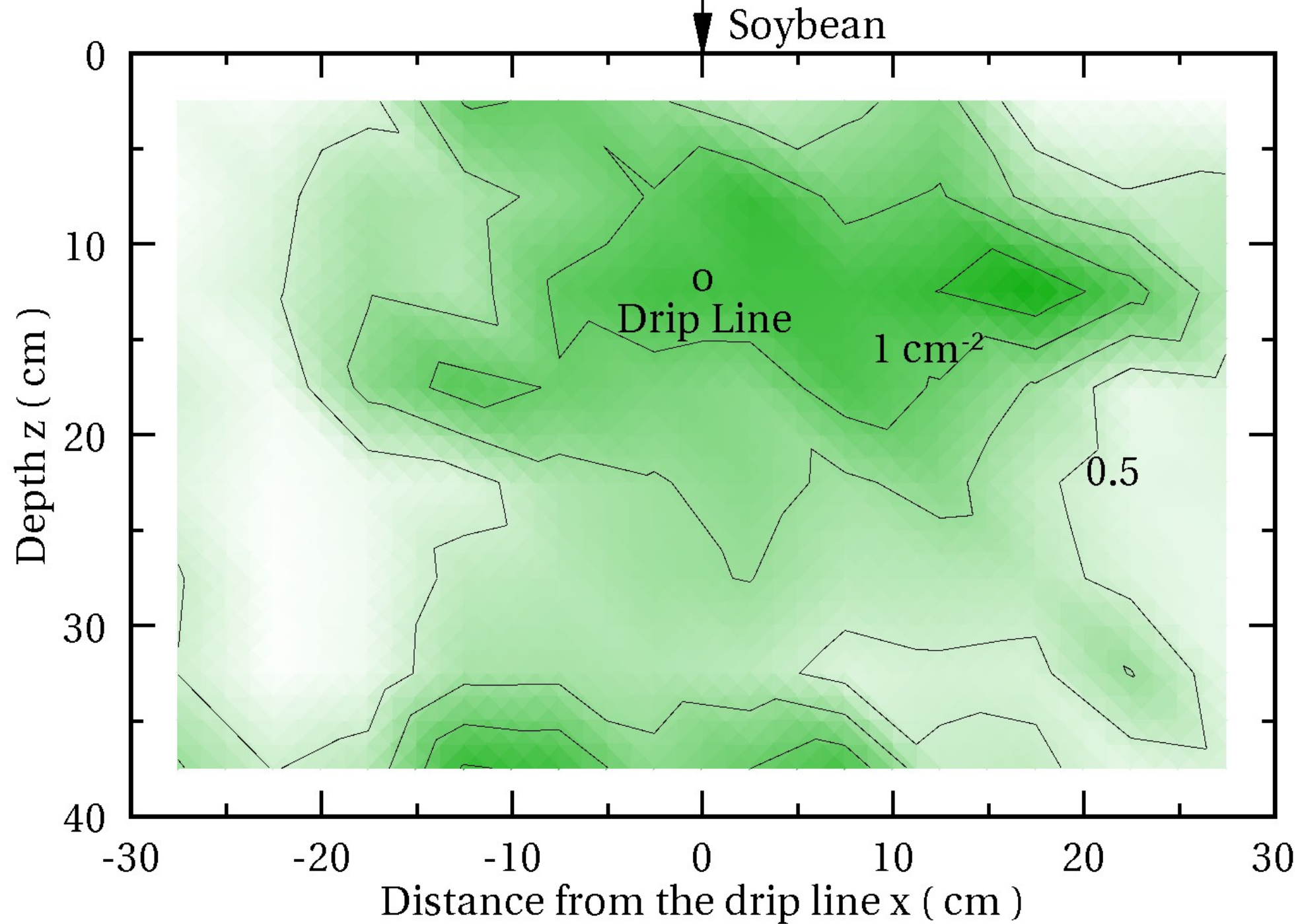
dt = 0.00238  
solute mass balance error = -0.080%  
s\_storage = 793.309  
cum\_s\_input = 262.455  
C[nx/2,1] = 102.300  
C[nx/2,nz] = 4.708  
C[nx/2,nz/2] = 5.791  
C[nx,1] = 102.300  
C[nx,nz] = 2.024  
Crystl[8,1] = 0.453



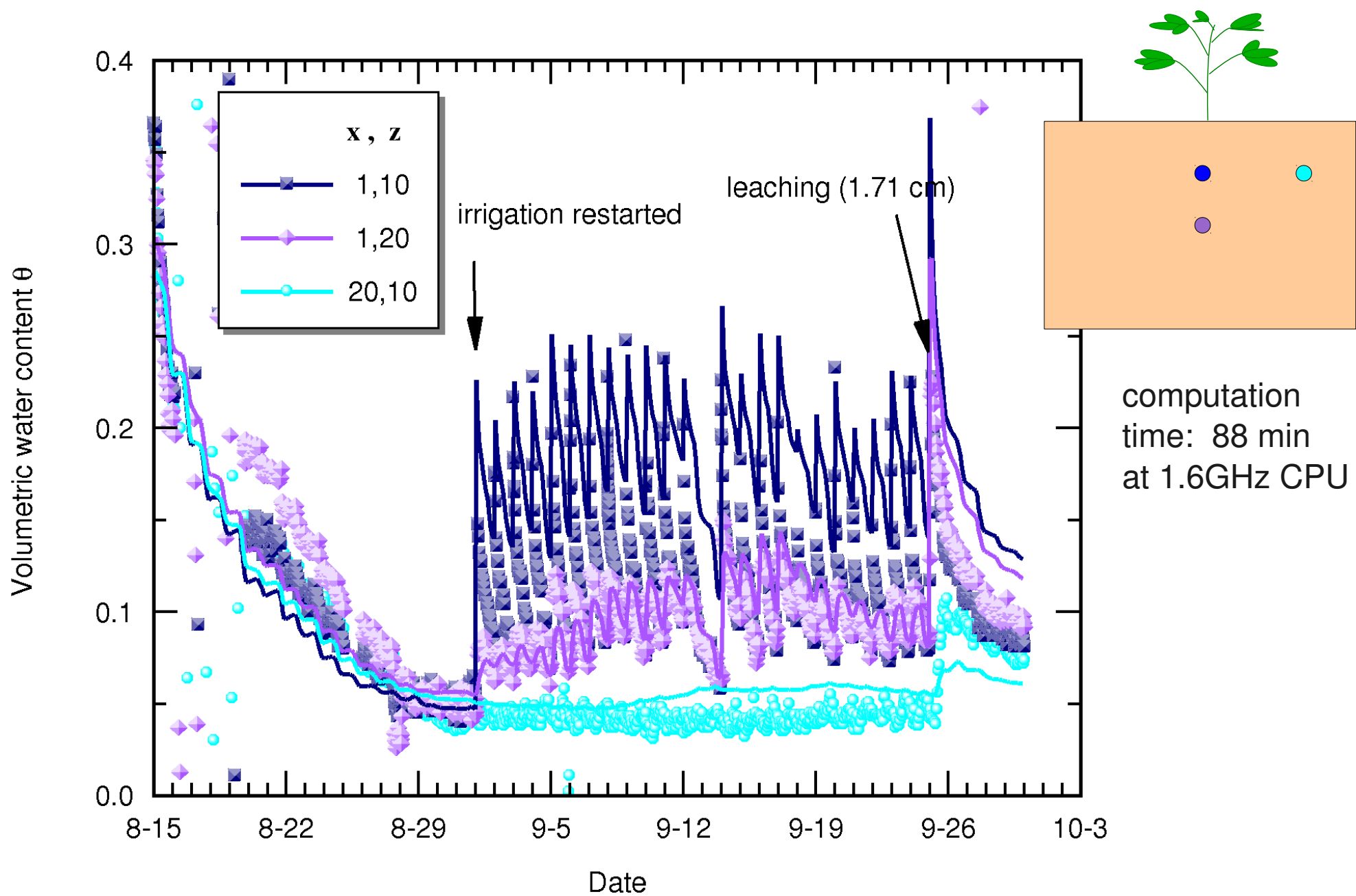
# Results and Discussion



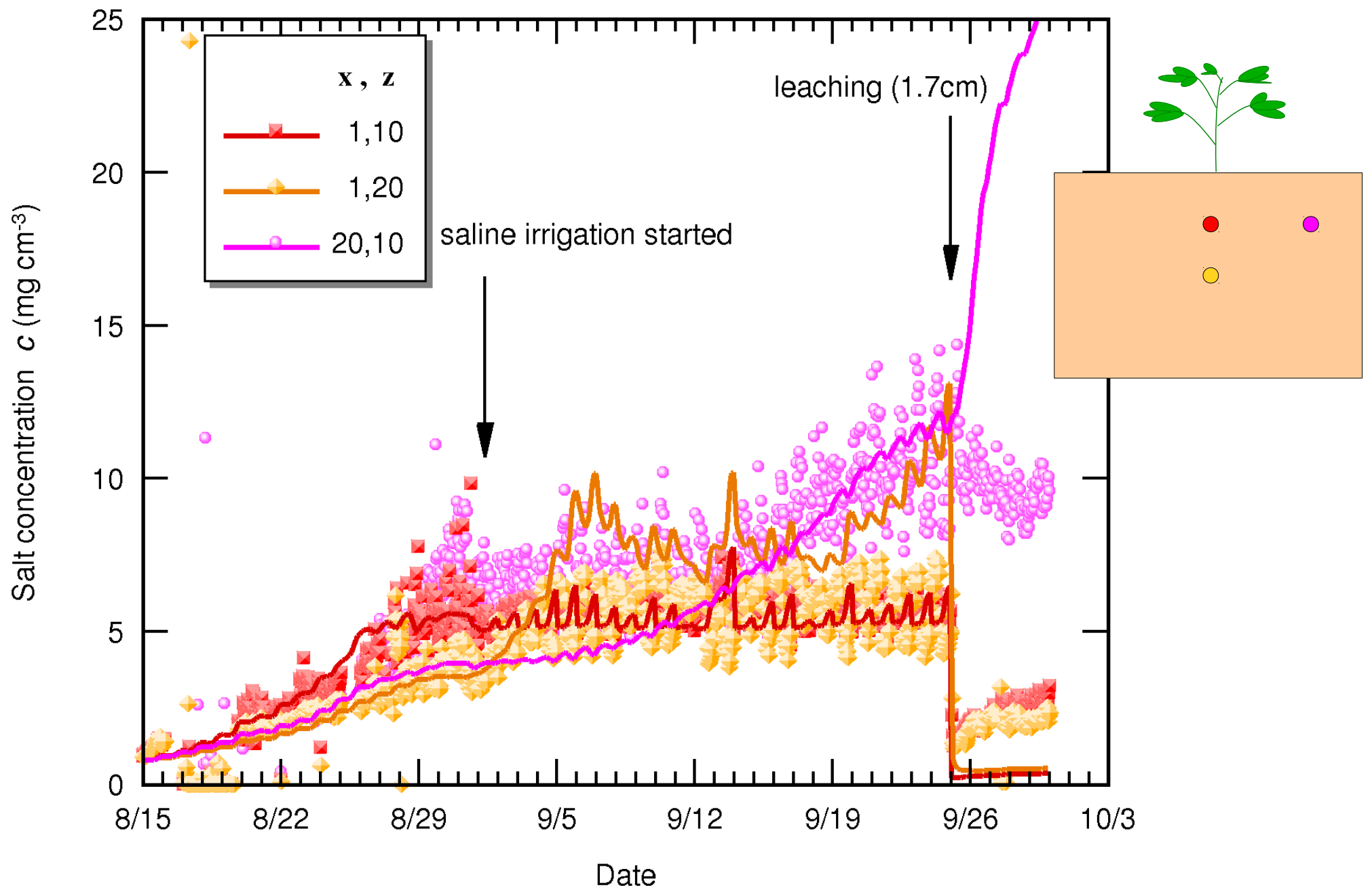
Comparison of measured and simulated time evolutions of



Root length density distribution  
in a vertical section at the end of the experiment 09A.

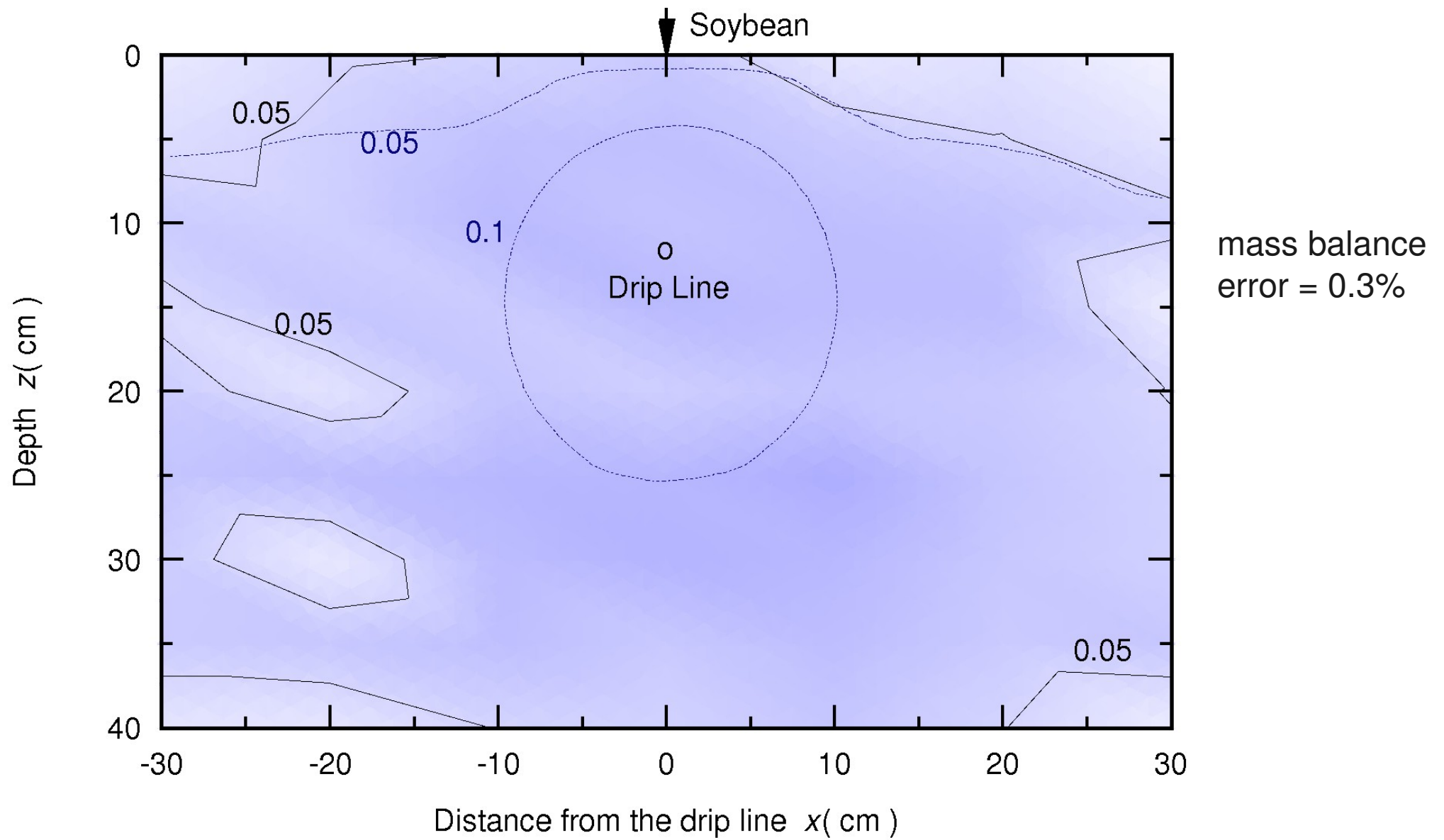


Comparison of measured (markers) and simulated (lines) time evolution of water content

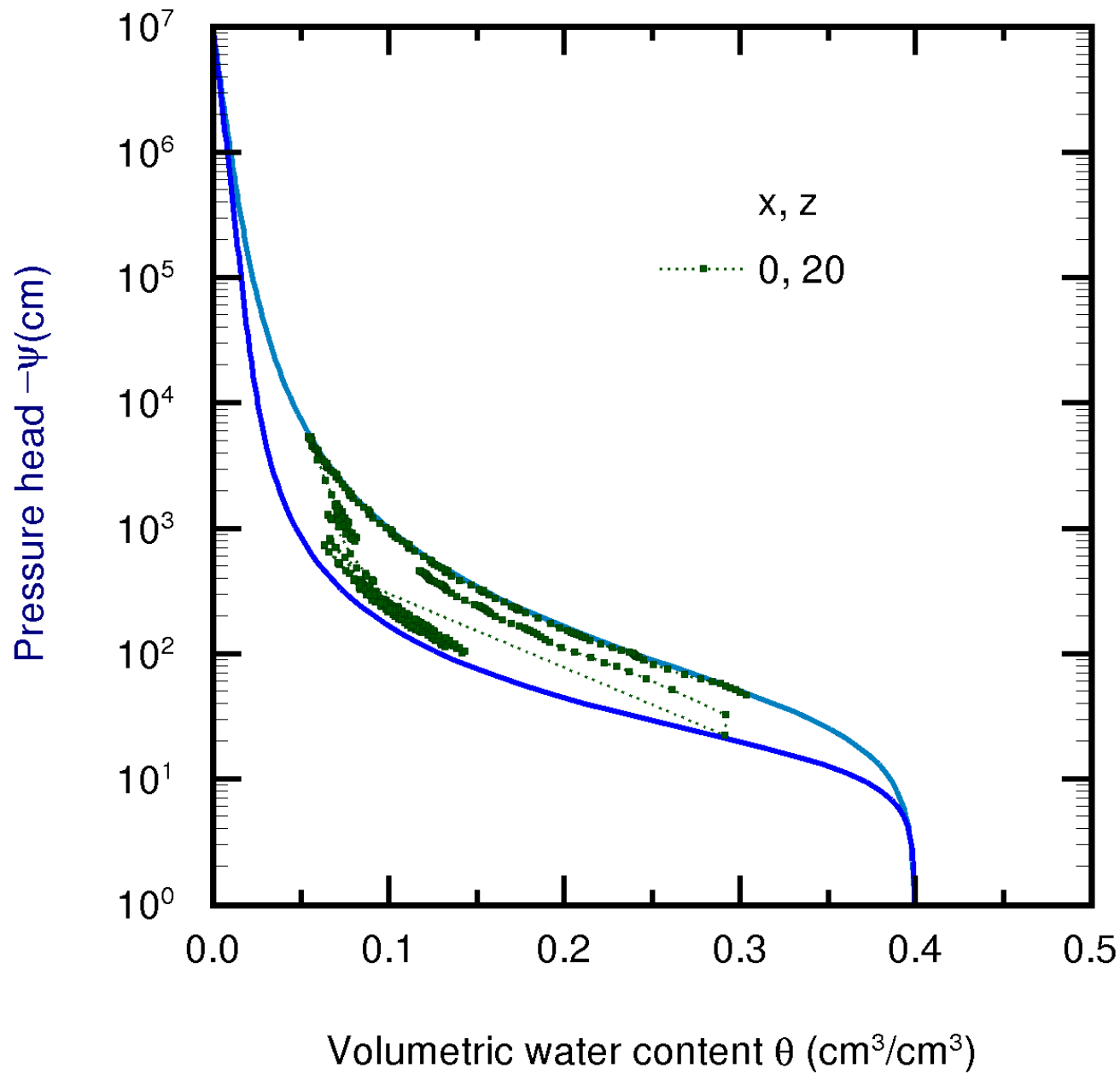


Comparison of measured (markers) and simulated (lines) time evolution of salinity





Comparison of measured and simulated volumetric water content distribution in a vertical section at the end of the experiment

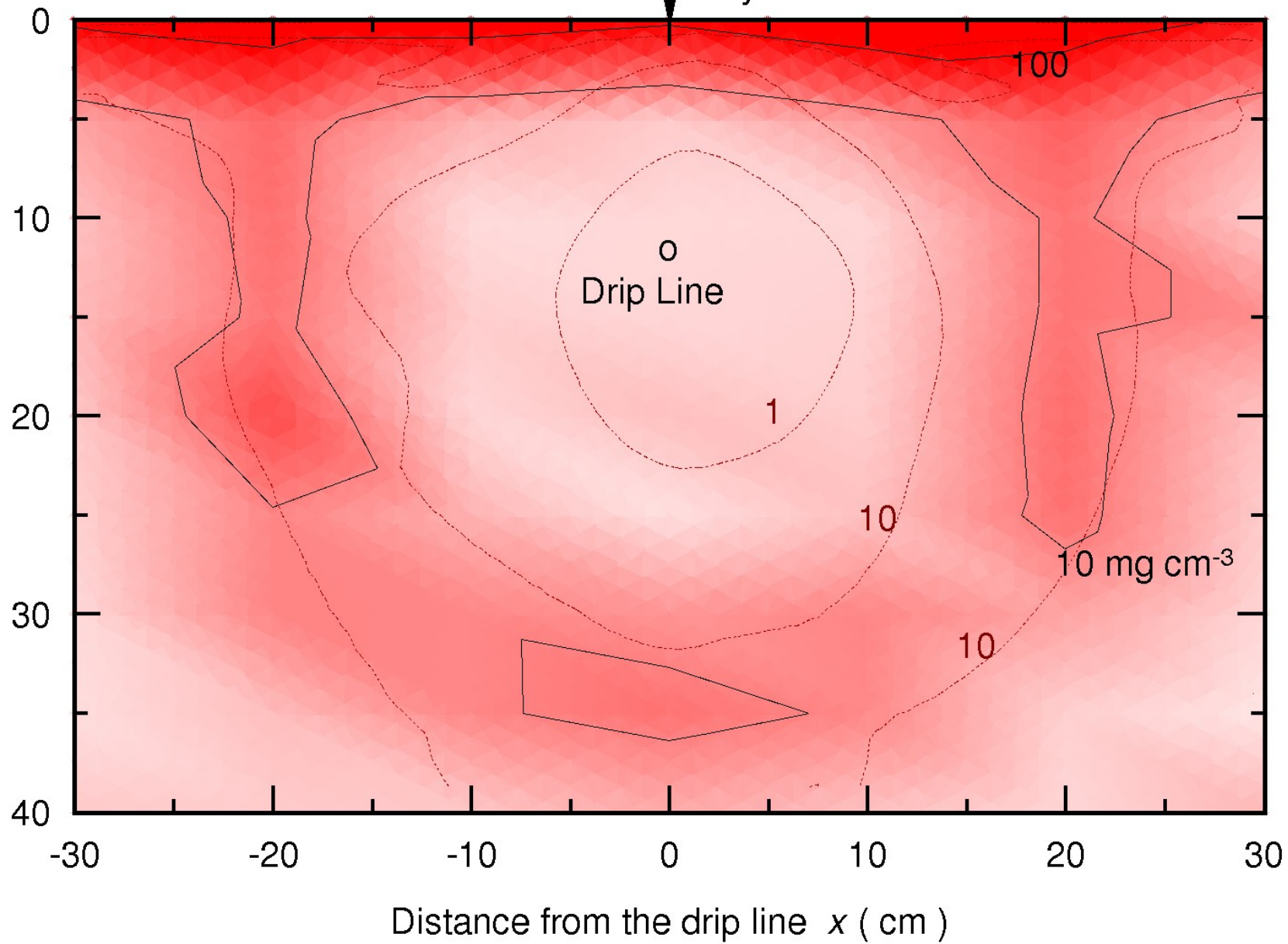


Underestimated K?

compensated root  
water uptake?

Simulated scanning curve at for Masa loamy sand

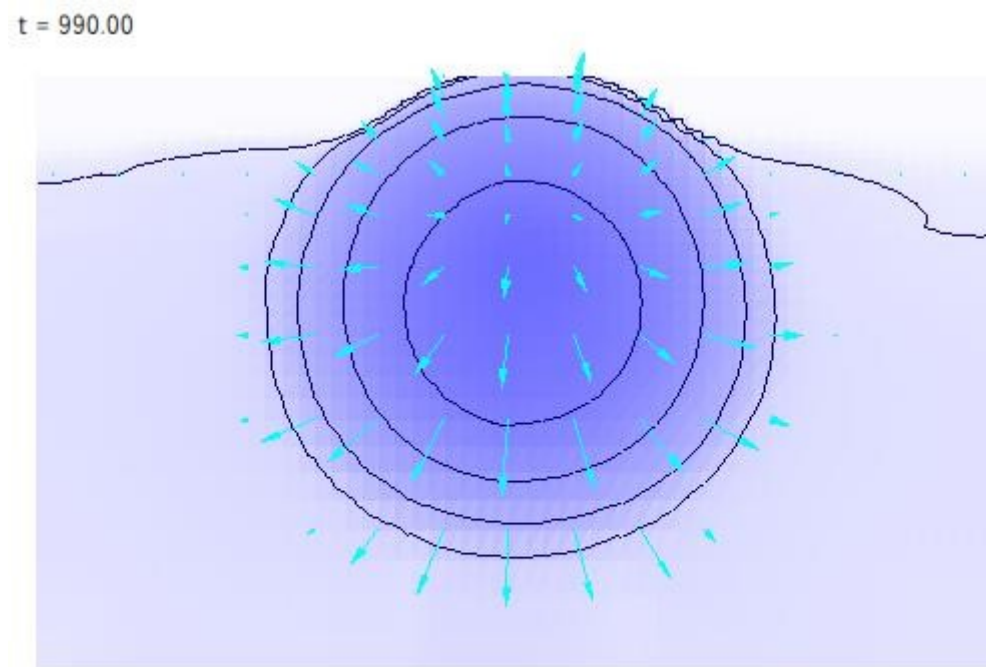
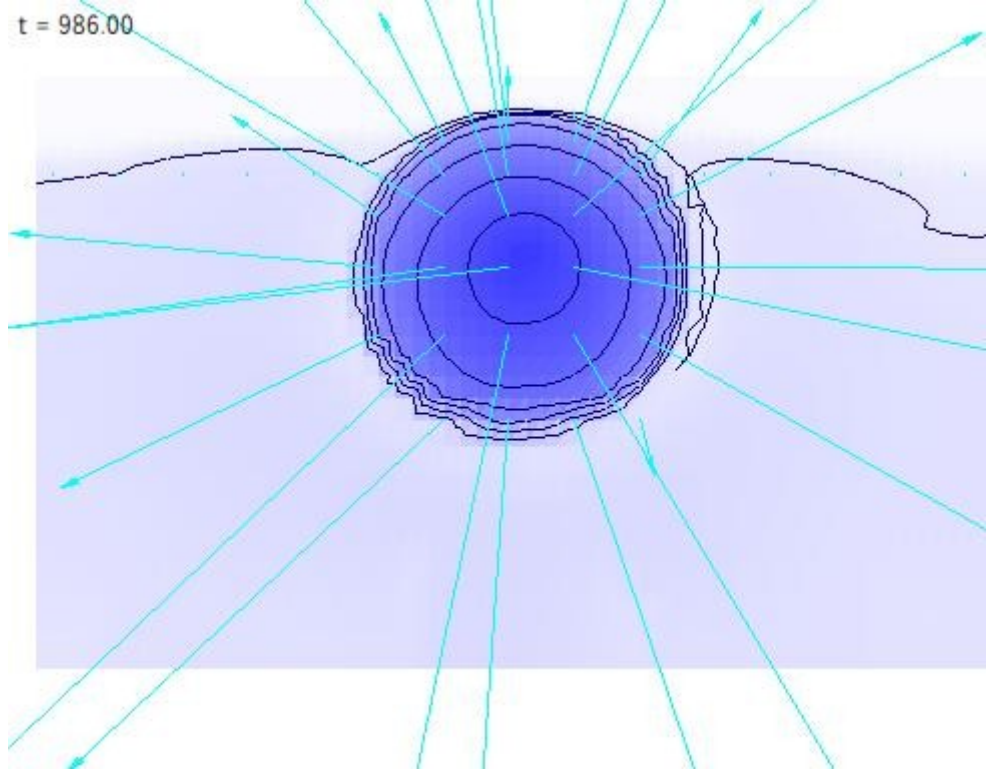
Soybean

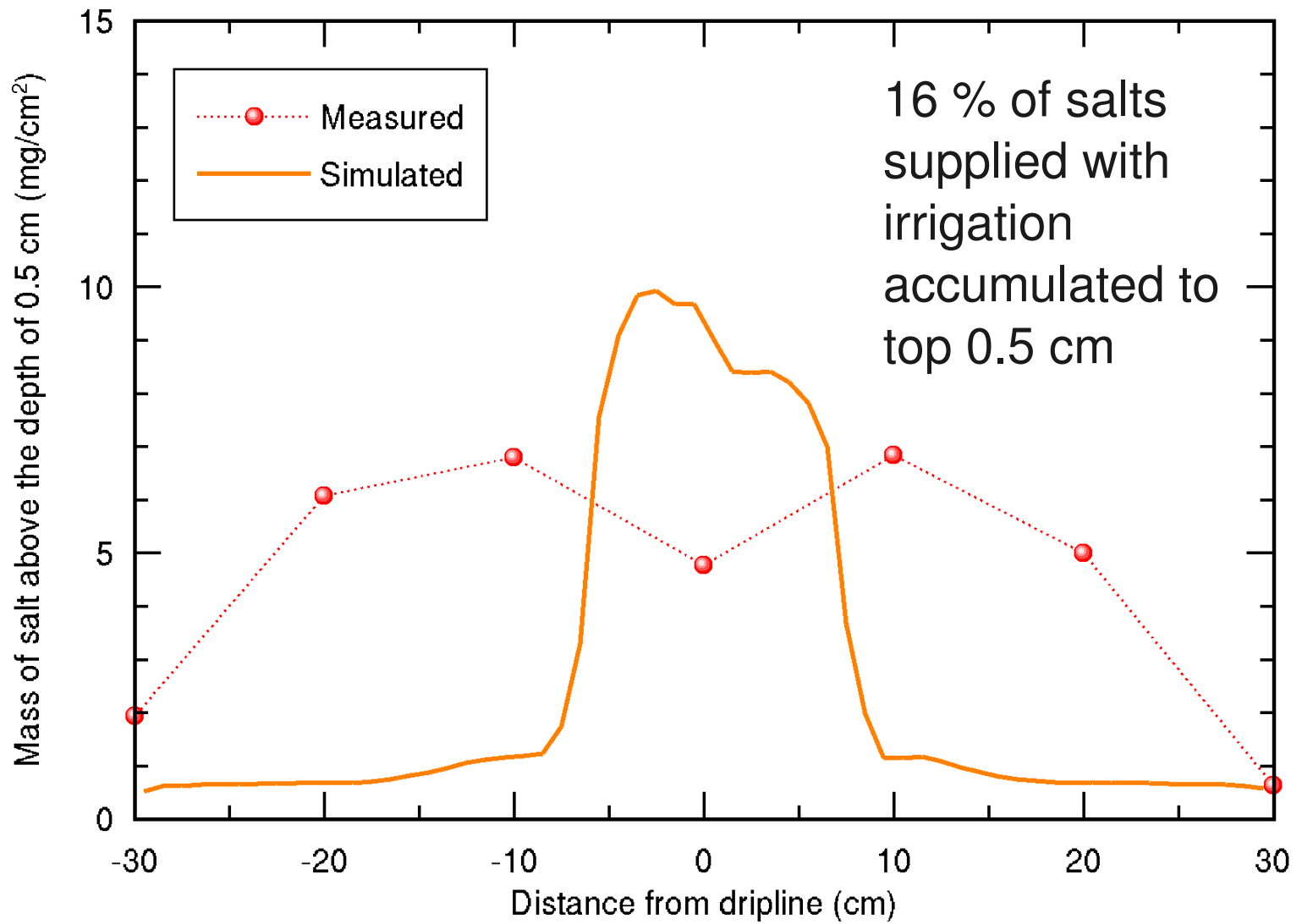


mass balance  
error = 0.7%

Comparison of measured and simulated salt concentration  
at the end of the experiment







Salt distribution along the soil surface at the end

## Conclusion

- Software for predicting two dimensional movement of water and solute considering the water vapor movement has been developed.
- Simulated values were in fair agreement, but further investigation is required to improve accuracy.
- Salts in the upper root zone was transported to the soil surface and a part of them was effectively removed by scraping top 0.5 cm layer.



*Thank you for your attention*







# Atmospheric Boundary Condition

$$E = \frac{\rho_{vs}^* h_{rs} - \rho_{va}^* h_{ra}}{r_a + r_{sc}}$$

$$h_{rs} \approx h_{re} = \exp\left(\frac{\psi_w}{R_v T}\right)$$

$\rho_v^*$  : saturated water vapor density (g/cm<sup>3</sup>)

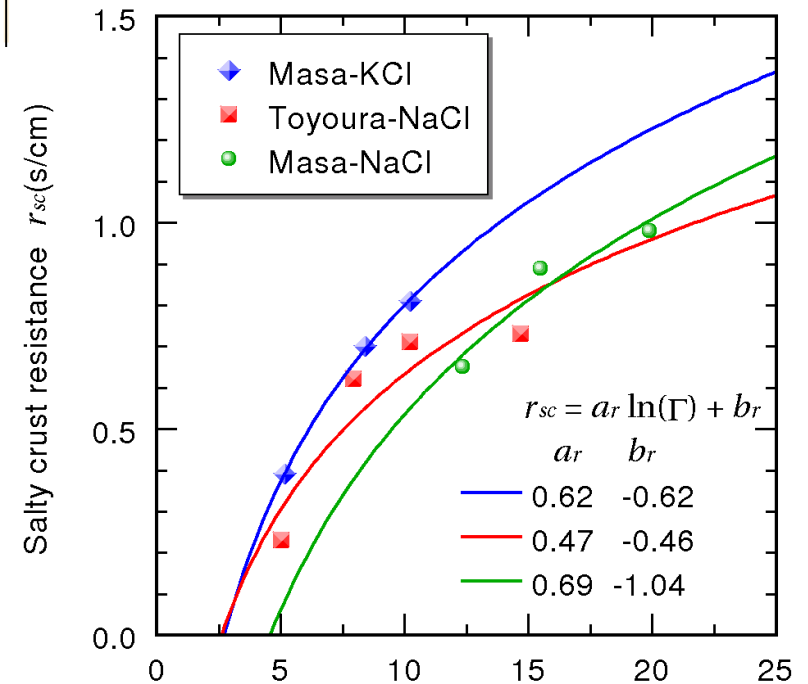
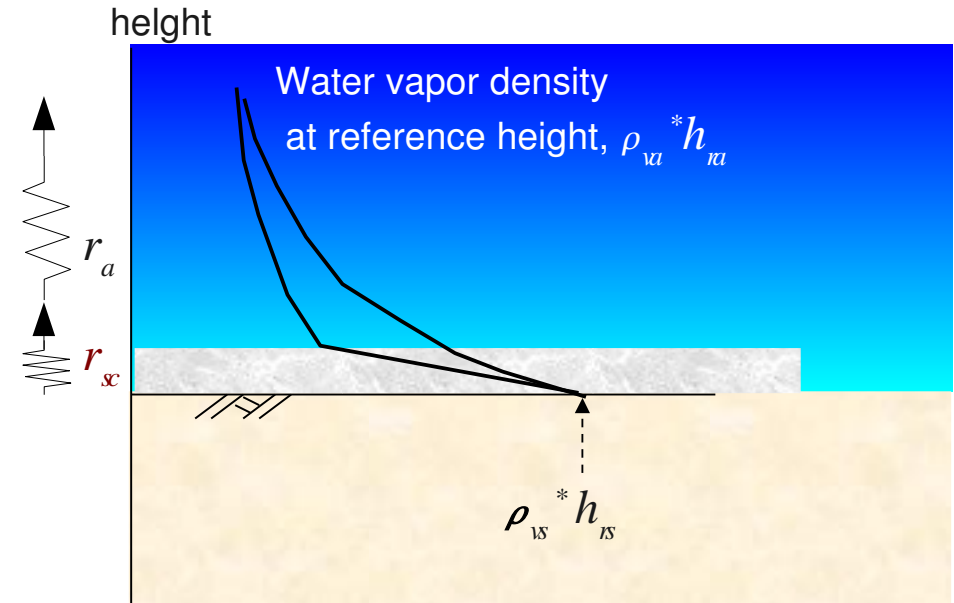
$h_r$  : relative humidity

$r_a$  : aerodynamic resistance (s/cm)

$r_{sc}$  : **salty crust resistance (s/cm)**

$\psi_w$  : water potential (cm)

$R_v$  : the gas constant for water vapor (4697 cm/K)



Mass of accumulated salt in  $z < 0.25$  cm  $\Gamma$  (mg/cm<sup>2</sup>)

Salty crust resistance as a function of accumulated salt